

# MATHEMATICAL MODELING AND EXPERIMENTAL STUDIES OF HYDROGEN COMBUSTION IN MICROTUBULAR SOLID OXIDE FUEL CELLS

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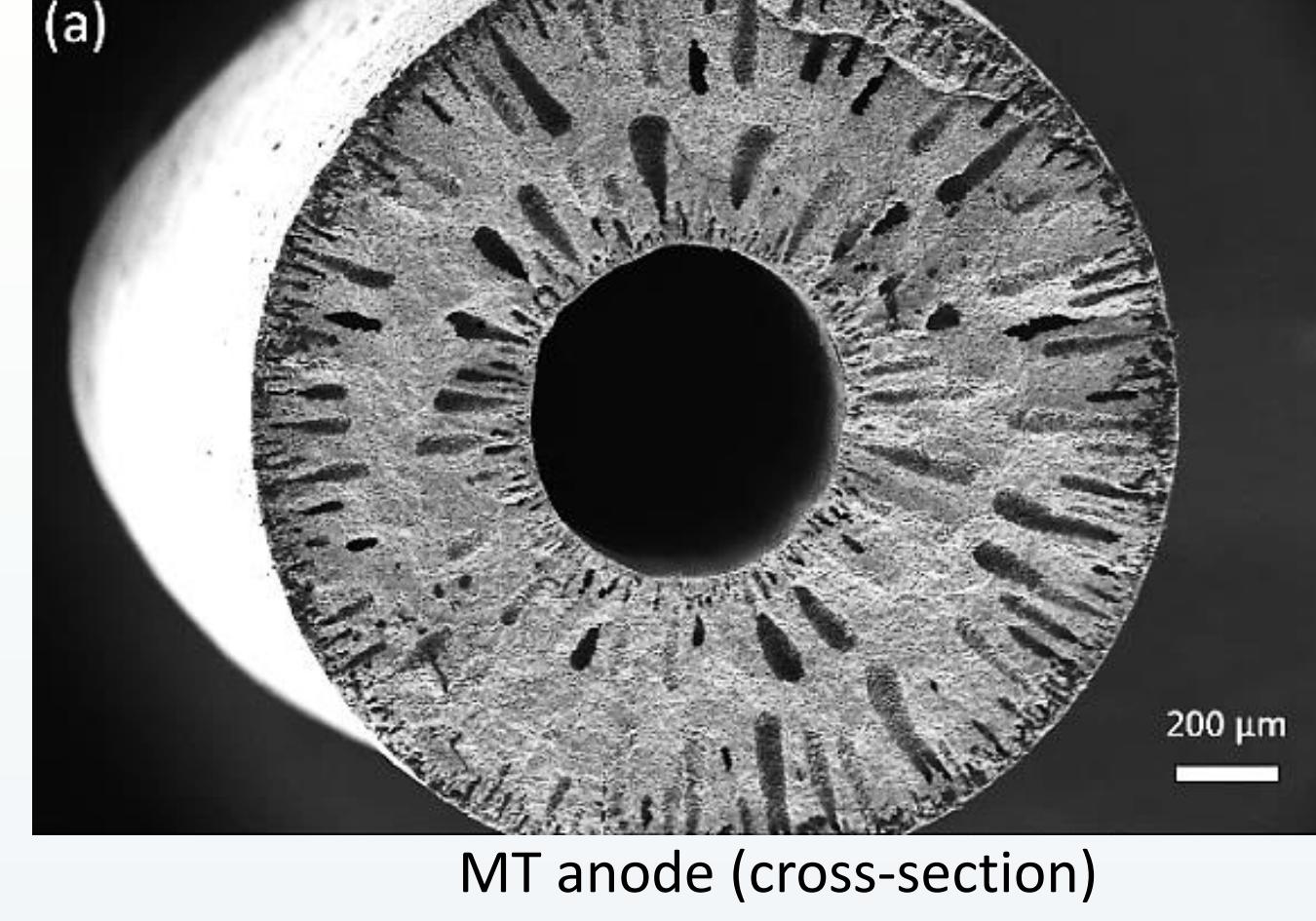


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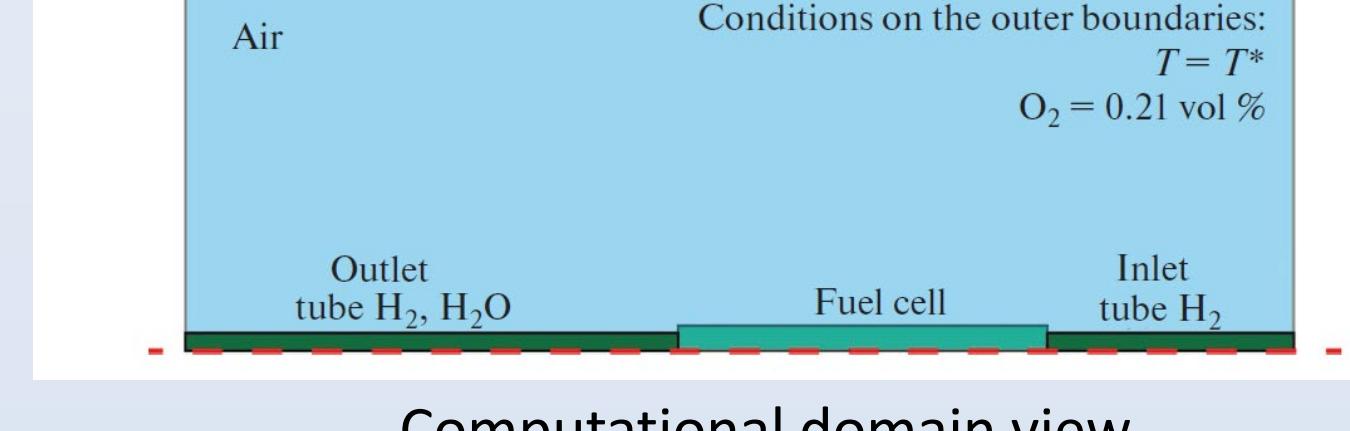
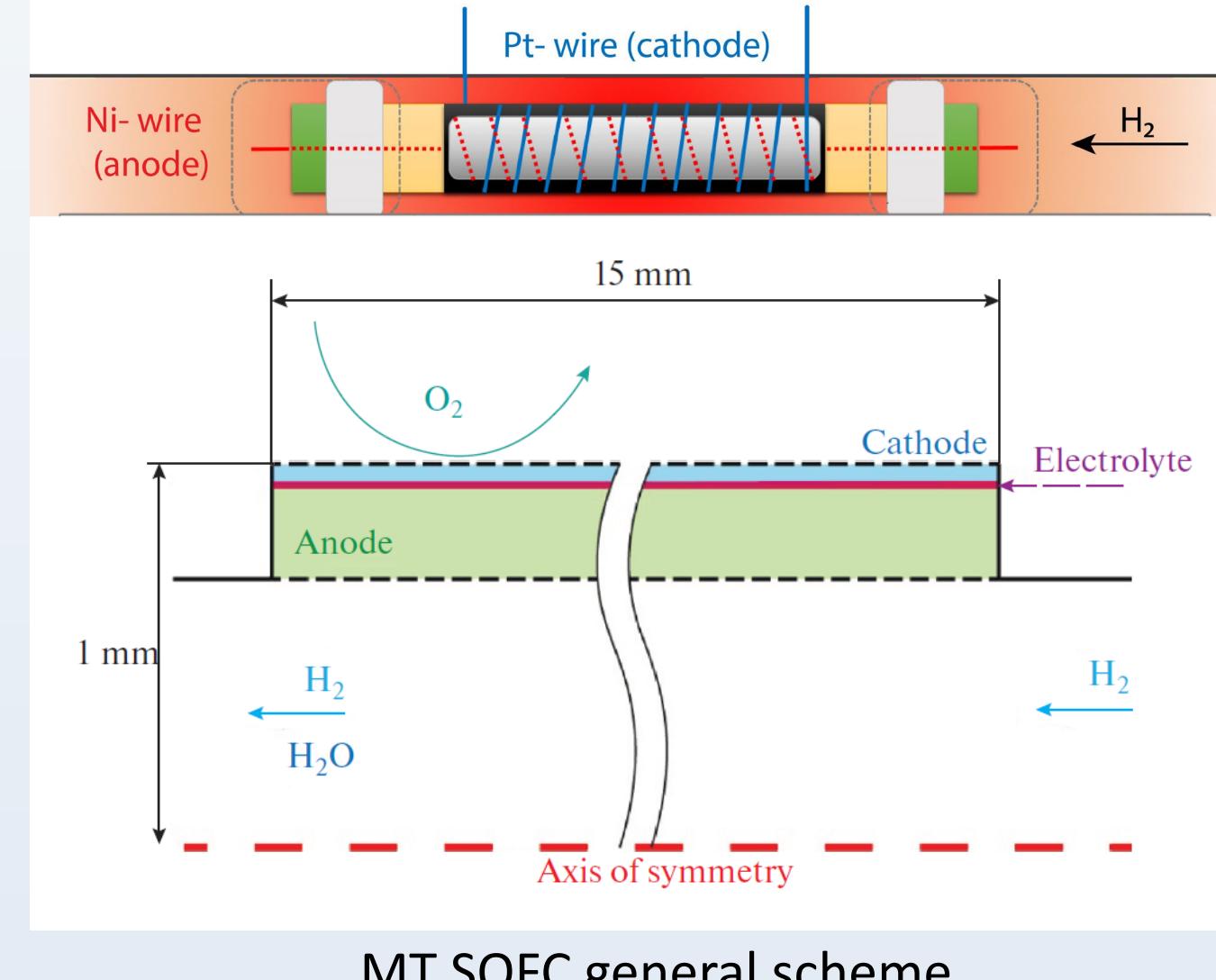
## MICROTUBULAR SOLID OXIDE FUEL CELLS:

- MT SOFCs – tubular elements whose outer diameter < 5 mm
- Gastight thin layer (electrolyte) sandwiched between porous layers (anode and cathode)
  - High oxygen flows
  - Mechanical strength
  - Thermal stress resistance
- Cathode and anode reactions:
  - $O_2 + 4\bar{e} \rightarrow 2O^{2-}$
  - $2H_2 + 2O^{2-} \rightarrow 2H_2O + 4\bar{e}$
- The limiting factor in MT SOFC wide application in electrical devices is reactor design and performance
- The mathematical modeling is meant to help this problem solution



## Mathematical model (COMSOL Multiphysics, 2D-axisymmetric geometry):

- Species transport (free and porous media):
  - $\nabla \cdot j_i + \rho(u \cdot \nabla)\omega_i = 0$
  - $j_i = -\left(\rho\omega_i \sum_k D_{ik} \left[\nabla x_k + \frac{1}{p}((x_k - \omega_k)\nabla p)\right]\right)$
  - $x_k = \frac{\omega_k}{M_k} M_n, \quad M_n = \left(\sum_i \frac{\omega_i}{M_i}\right)^{-1}$
  - Boundary reaction
    - $-n \cdot j_i = \sum_k M_i R_{i,k}$
- Species transport (electrolyte):
  - $-\nabla \cdot (D_{O2}^s \nabla c^-) = 0$
  - Boundary reaction
    - $-n \cdot j_i = \sum_k R_{i,k}$
- Momentum balance (free and porous media)
  - $\rho(u \cdot \nabla)u = \nabla \cdot \left[-pI + \mu(\nabla u + (\nabla u)^T) - \frac{2\mu}{3}(\nabla \cdot u)I\right]$
  - $\nabla \cdot (\rho u) = 0$
- Heat balance
  - $\rho C_P u \cdot \nabla T - \nabla \cdot ((1 - \varepsilon_p)\lambda_s + \varepsilon_p \lambda) \nabla T = 0$
  - Boundary reaction heating
    - $-n \cdot q = Q$



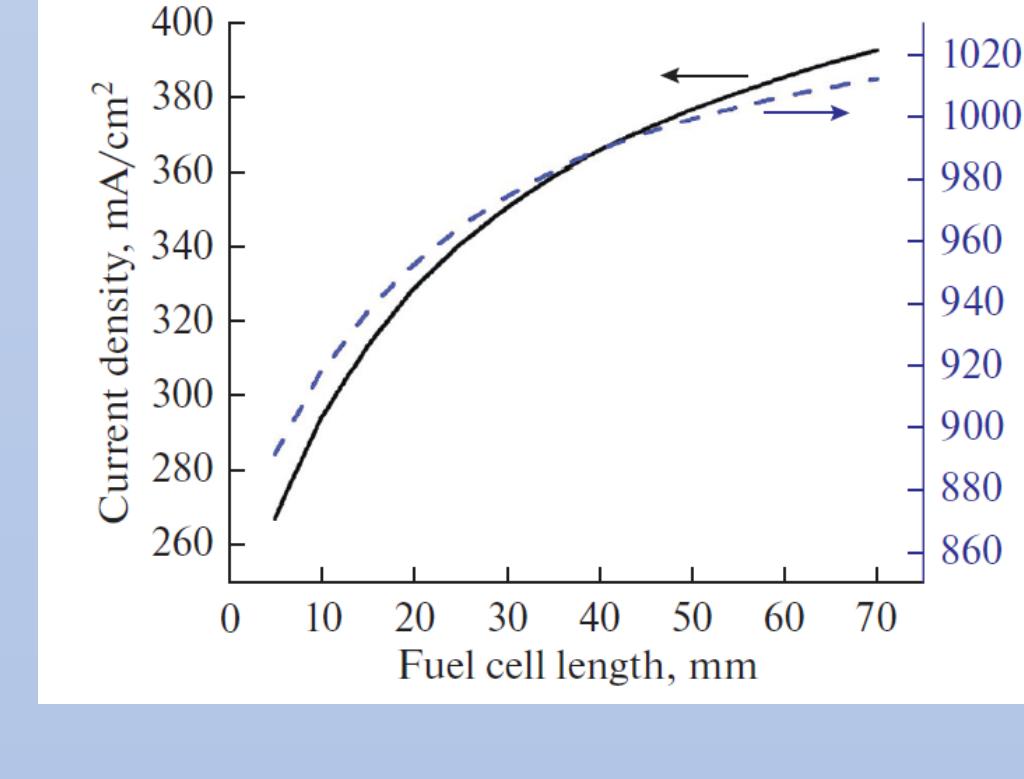
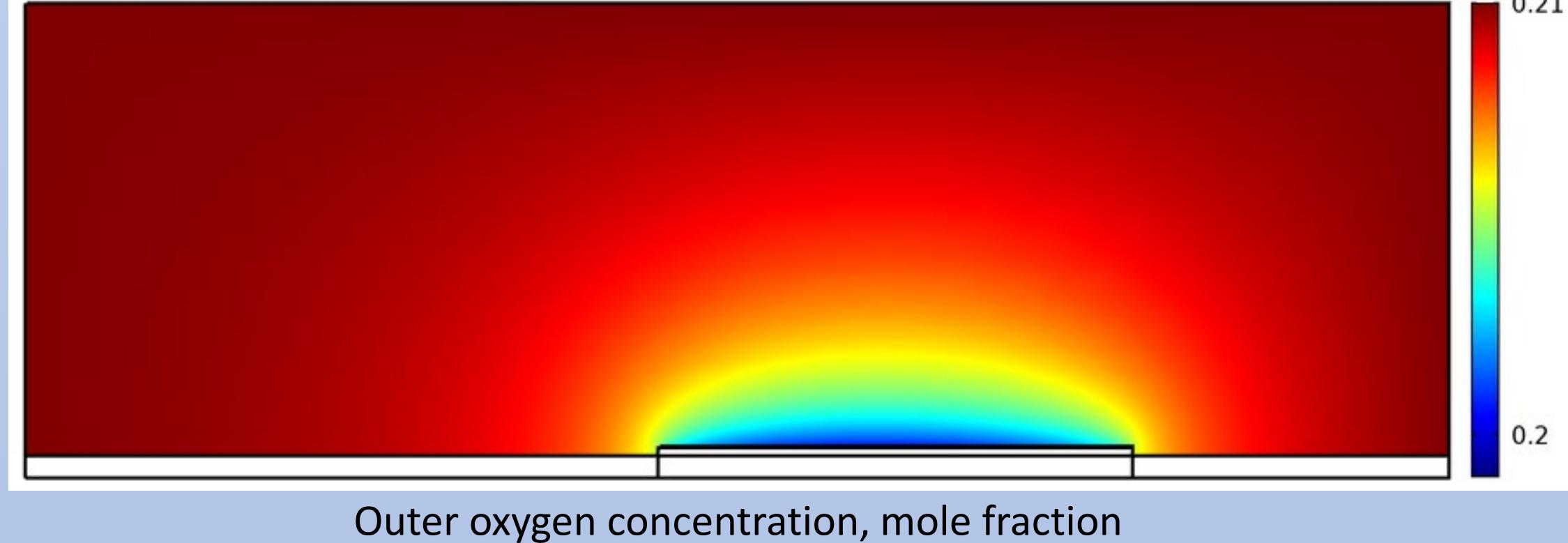
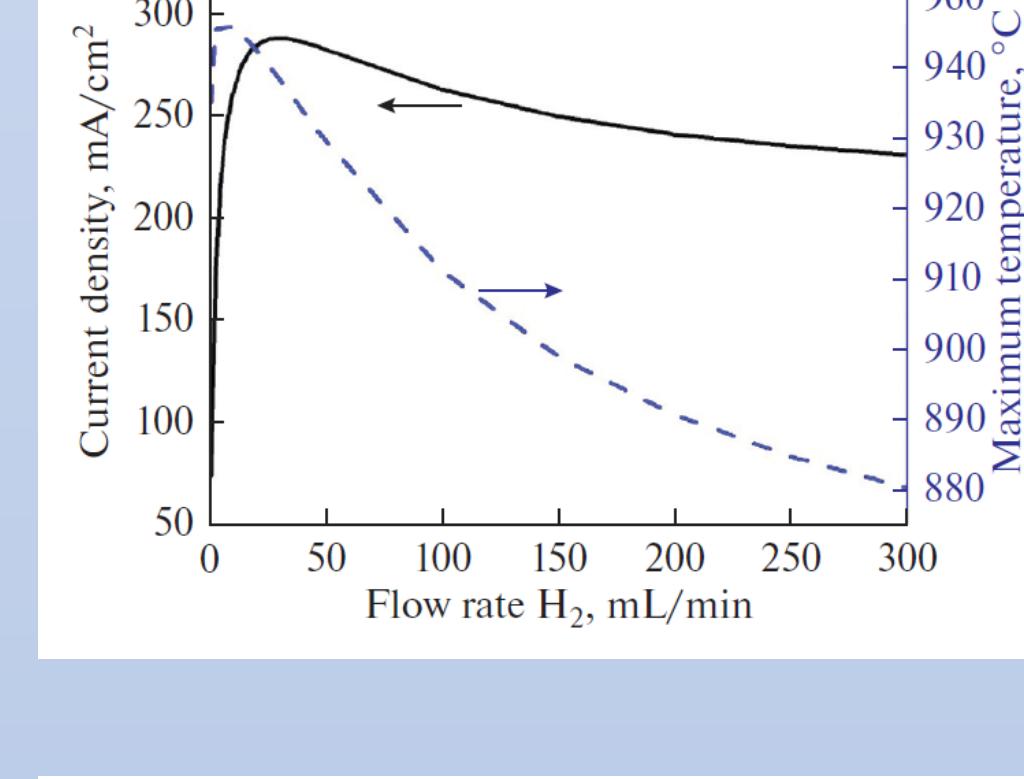
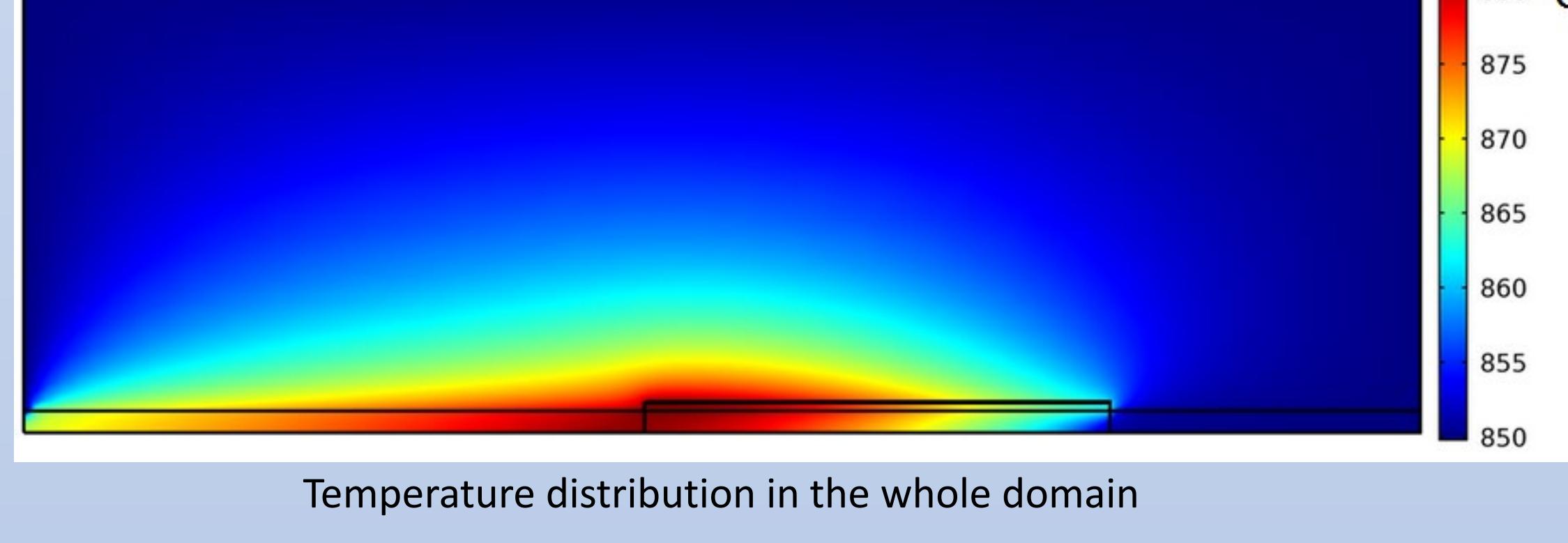
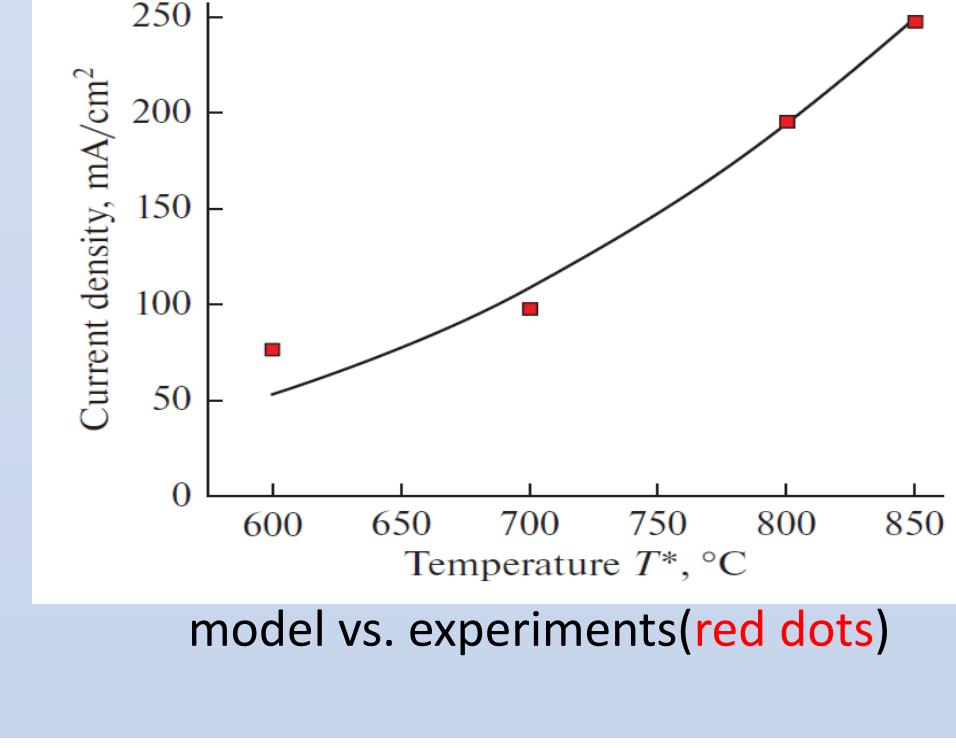
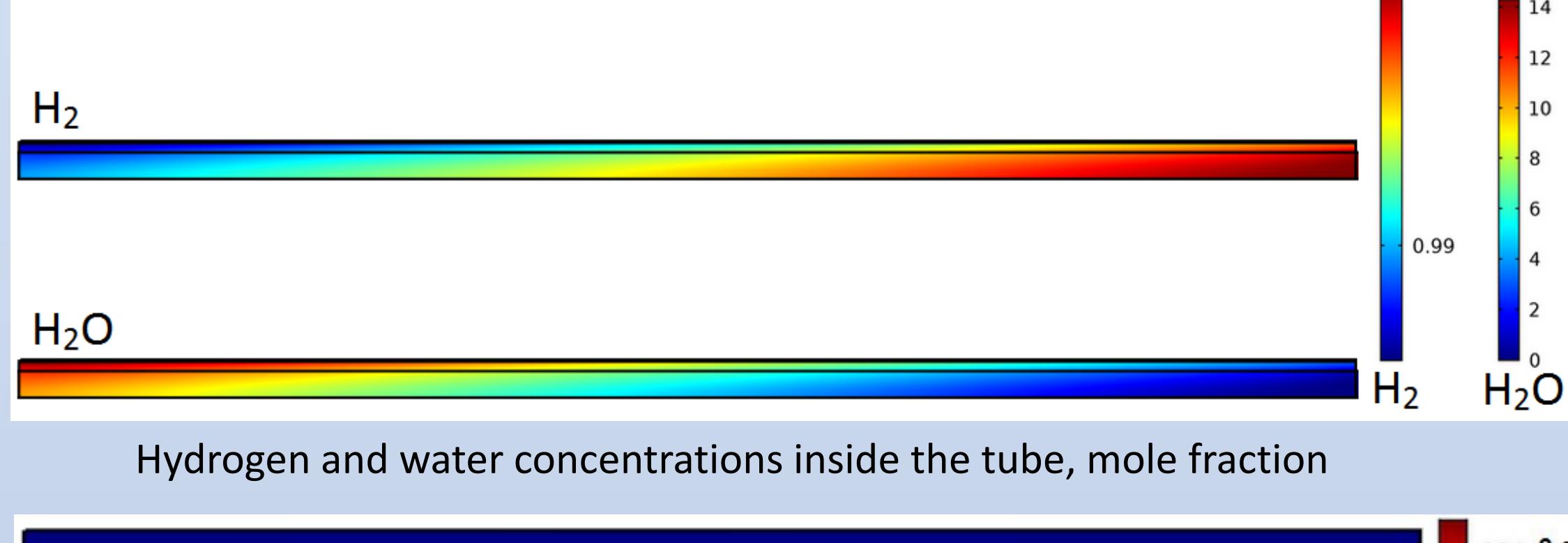
i	1	2	eq
$E_i, \text{J/mol}$	40 000	70 000	2 365
$k_i^0$	1, mol/m <sup>2</sup> /s	10, m/s	20 800

Estimated kinetic parameters

## Model parameters:

- Gas inlet conditions:
  - H<sub>2</sub> inlet concentrations – 1 mole fraction
  - Gas flow rate 300 ml/min
  - 600 < T\* < 850
- Reaction rates:
  - $R_1 = k_1 \left(c_o - \frac{c^-}{k_{eq}}\right)$
  - $R_2 = k_2 x_H c^-$
- Solid-phase diffusivity
  - $D_{O2}^s = 1.5 \times 10^{-8} \exp(-8120/T) \text{ m}^2/\text{s}$

## RESULTS (T\* = 850 °C):



- Conclusion
  - High hydrogen flow rate leads to current density decreasing
  - Too long tubes may lead to overheating